# Ab Initio Study of the Ammonia-Ammonia Dimer: BSSE-Free Structures and Intermolecular Harmonic Vibrational Frequencies 

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#### Abstract

The influence of basis set superposition error (BSSE) in optimized geometries, force constants and intermolecular harmonic vibrational frequencies of the ammonia-ammonia dimer have been studied both at the Hartree-Fock and correlated (second-order Moller-Plesset perturbation theory) levels of theory using several different basis sets as ( $6-31 \mathrm{G}, 6-311 \mathrm{G}, 6-31++\mathrm{G}, 6-311++\mathrm{G}, 6-31 \mathrm{G}(\mathrm{d}, \mathrm{p}), 6-311 \mathrm{G}(\mathrm{d}, \mathrm{p})$, $6-31++G(d, p) 6-311++G(d, p)$ and $6-311++G(2 d, 2 p))$. The widely used a posteriori Boys-Bernardi "counterpoise" (CP) correction scheme has been compared with the a priori method utilizing the chemical Hamiltonian approach (CHA). The results show that practically there is no difference between these two methods, so the a priori CHA scheme can be considered as an ultimate solution of the BSSE problem. It is also concluded that the BSSE influence is very significant, so removing this effect is very important. © 2004 Wiley Periodicals, Inc. Int J Quantum Chem 99: 585-593, 2004


Key words: basis set superposition error; chemical Hamiltonian approach; harmonic vibrational frequencies; intermolecular interactions

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## 1. Introduction

Recently a number of different theoretical [1-8] and experimental [9-16] methods have been developed to study the structures of the am-monia-ammonia hydrogen-bonded complex. Considering the experimental data, it has been generally accepted that the ammonia dimer may have a linear hydrogen-bonded structure, but in 1985 Nelson et al. [11] gave strong evidence for a cyclic rather than linear structure by microwave study. On the other hand, the theoretical studies showed that one can find stationary points on the $\mathrm{NH}_{3}-\mathrm{NH}_{3}$ with two $C_{s}$ and $C_{2 h}$ symmetries [4], respectively. In 1994 Olthof et al. [12] proposed a new potential with parameters for ammonia dimer by calculating the six-dimensional vibration-rotation-tunneling states, which were constructed from previous ab initio results and also were adjusted to reproduce the interchange splittings in the far-infrared (FIR) spectrum. Using this new potential it was possible to explain the existing experimental FIR data and other observed properties such as the decreased dipole moment of $\left(\mathrm{ND}_{3}\right)_{2}$ compared to $\left(\mathrm{NH}_{3}\right)_{2}$. The Olthof's potential shows that the ammonia dimer has an intermediate structure between the centrosymmetric cyclic and the linear hydrogenbonded structure which could not have been obtained before by pure ab initio study. Almost all the theoretical (perturbational and density functional theories) studies have shown a linear hydrogenbonded structure, except Lee and Park's work [4] who predict the aforementioned intermediate structure using a series of correlation consistent basis sets, cc-pVXZ and aug-cc-pVXZ $(X=D, T, Q)$ at the Hartree-Fock (HF), second-order and fourth-order Møller-Plesset perturbation theory (MP2, MP4) levels.

The potential energy surface appears to be very flat near its equilibrium structure, and the values of the equilibrium energies belonging to the different symmetries are very close to each other and depend strongly upon the basis sets and the methods applied. The focal point of these studies was to find the global equilibrium structure and characteristic features of the PES of these dimers. In this paper, we examine the BSSE effects of equilibrium structures, force constants and harmonic vibrational frequencies of the ammonia-ammonia dimer using Hartree-Fock method and Møller-Plesset perturbation theory. Our aim is to give a better and much more accurate description for these quantities. Most
of the calculations for the hydrogen-bonded complexes are based on the supermolecular approach, in which the interaction energy of the dimer is obtained as an energy difference between the supermolecule and the monomers. However, this interaction energy often shows minima that are too deep, especially for the case of weakly bonded intermolecular systems, as a consequence of using finite basis sets in the calculations. This phenomenon is called "basis set superposition error," and it is due to the fact that the description of the monomer is actually better within the supermolecule than that which one has for the free monomers by applying the same basis set. So, the BSSE is a purely "mathematical effect" that appears only due to the use of finite basis sets, leading to an incomplete description in the individual monomers. Several numerical studies and analytical considerations [17-19] show that the magnitude of this BSSE effect can be very large even for fairly large basis sets, so removing it in the practical calculations is very important. Different techniques have been proposed [20-26] to correct this artificial effect.

More than 30 years ago, Jansen and Ros [20] and, independently, Boys and Bernardi [21] suggested an a posteriori "counterpoise correction" (CP) scheme of calculating the monomer energies in the same basis set as used for the supermolecule. This means that the description of the monomers is adjusted to the dimer problem, and the energies and other quantities of the free monomers become dis-tance-dependent.

In 1983, Mayer proposed a new a priori procedure to tackle the BSSE problem. This is the socalled "chemical Hamiltonian approach" (CHA) [27, 28], which permits one to identify those terms of the Hamiltonian that are responsible for the BSSE effects. By omitting these terms, one can obtain wave functions that are free from artificial nonphysical delocalizations. Using this CHA scheme, several different approaches have been developed both at the HF [29-39] and correlated [40-47] levels of theory.

According to previous studies, the results obtained from the Boys-Bernardi and CHA methods are very close to each other, despite the fact that these schemes are conceptually very different. In this work, we apply both methods in order to study the structures, the force constants and harmonic vibrational frequencies of the ammonia-ammonia hydrogen-bonded complex. Similar studies have been performed in an our earlier work [48] for the hydrogen fluoride and water dimers.

The methods employed (CP, CHA/CE, and CHA/MP2) are briefly explained in the section 2 . In section 3, the results for the ammonia-ammonia dimer are presented in several different basis sets, and the force constants and harmonic vibrational frequencies obtained are compared and discussed. The conclusions of the paper are given in the final section.

## 2. Methods Applied (CP, CHA/CE and CHA/MP2)

In this section, the CP and CHA methods presented in earlier papers [20,21,27] are briefly reviewed.

### 2.1. CP SCHEME

The most popular posteriori method correcting the BSSE is the Boys-Bernardi counterpoise correction (CP) scheme introduced by Jansen and Ross [20] and, independently, by Boys and Bernardi [21]. Applying this CP scheme one has to recalculate the monomers in the basis of the whole supermolecule for every geometrical arrangement. The CP-corrected interaction energy $\Delta E^{\mathrm{CP}}$ can be defined as the difference of the supermolecule and monomer energies, all computed in the same supermolecule basis set:

$$
\begin{equation*}
\Delta E_{A B}^{C P}=E_{A B}(A B)-E_{A}(A B)-E_{B}(A B) \tag{1}
\end{equation*}
$$

The uncorrected binding energy $\Delta E^{\text {unc. }}$ can be obtained as

$$
\begin{equation*}
\Delta E_{A B}^{\text {unc. }}=E_{A B}(A B)-E_{A}(A)-E_{B}(B) . \tag{2}
\end{equation*}
$$

Using Eqs. (1) and (2), one can define the BSSE content in the interaction energy as

$$
\begin{align*}
\delta E_{\text {BSSE }}=\Delta E_{A B}^{\text {unc. }}-\Delta E_{A B}^{\mathrm{CP}}=E_{A} & (A B)-E_{A}(A) \\
& +E_{B}(A B)-E_{B}(B) . \tag{3}
\end{align*}
$$

According to the Eq. (3), the CP-corrected potential energy surface (PES) of the dimer becomes

$$
\begin{align*}
E^{\mathrm{CP}}(A B)=E_{A B}^{\mathrm{unc} \cdot}(A B) & -\delta E_{\mathrm{BSSE}}=E_{A B}^{\mathrm{unc} \cdot}(A B)-E_{A}(A B) \\
& +E_{A}(A)-E_{B}(A B)+E_{B}(B) . \tag{4}
\end{align*}
$$

Using Eq. (4), in addition to the monomer energies one has to calculate three different energy values [29] at every geometrical arrangement of the system in order to determine the CP-corrected PES.

### 2.2. CHA SCHEME

A conceptually different way of handling the BSSE problem is to apply the a priori "chemical Hamiltonian approach" (CHA) introduced by Mayer [27, 28]. The CHA procedure permits the supermolecule calculations to keep consistency with those for the free monomer performed in their original basis sets. The most important aspect of Mayer's scheme is that one can devide the Hamiltonian into two parts and omit those terms that are responsible for the BSSE:

$$
\begin{equation*}
\hat{H}_{\mathrm{BO}}=\hat{H}_{\mathrm{CHA}}+\hat{H}_{\mathrm{BSSE}} . \tag{5}
\end{equation*}
$$

Here $\hat{H}_{\mathrm{BO}}$ is the original Born-Oppenheimer Hamiltonian, $\hat{H}_{\text {CHA }}$ is the BSSE-free part of the Hamiltonian, while the second term on the right hand side corresponds to the BSSE. It must be emphasized that, as BSSE is not a physical quantity, one cannot expect the remaining part of the Hamiltonian $\hat{H}_{\text {CHA }}$ to be Hermitian. Applying this nonHermitian BSSE-free CHA Hamiltonian $\hat{H}_{\text {CHA }}$ and using the method of momenta instead of the variational principle appropriate Hartree-Fock type CHA-SCF [30] equations were derived in order to calculate BSSE-free wave functions:

$$
\begin{equation*}
\hat{H}_{\mathrm{CHA}} \Psi_{\mathrm{CHA}}=\Lambda \Psi_{\mathrm{CHA}} . \tag{6}
\end{equation*}
$$

As a result of several numerical and analytical considerations [34-37] using this BSSE-free wave function the energy of the system can be calculated as a conventional expectation value of the original Born-Oppenheimer Hamiltonian and not of the "chemical" one. (This is indicated by the expression "CHA with conventional energy," CHA/CE.) Here is our working formula:

$$
\begin{equation*}
E_{\mathrm{CHA} / \mathrm{CE}}=\frac{\left\langle\Psi_{\mathrm{CHA}}\right| \hat{H}_{\mathrm{B}}\left|\Psi_{\mathrm{CHA}}\right\rangle}{\left\langle\Psi_{\mathrm{CHA}} \mid \Psi_{\mathrm{CHA}}\right\rangle} . \tag{7}
\end{equation*}
$$

While obtaining Hartree-Fock-type equations from the CHA Hamiltonian is a relatively straightforward procedure, the generalization of it to the Moller-Plesset perturbation theory was a bigger task. As it was shown by Mayer [49], the appropri-
ate second-order energy can be obtained as follows. Firstly, one has to calculate the first-order CHA wave function $\chi$ by using the non-Hermitian Hamiltonian partitioned as $\hat{H}_{\text {CHA }}=\hat{H}^{0}+\hat{V}_{\text {CHA }}$, where $\hat{H}^{0}$ is the unperturbed Hamiltonian. The perturbed $\hat{V}_{\text {CHA }}$ operator is also non-Hermitian because it is built up of the nonorthogonal eigenvectors of the non-Hermitian CHA-SCF equations [30]. The original Hermitian Born-Oppenheimer Hamiltonian $\hat{H}_{\mathrm{BO}}$ can also be partitioned as a sum of the same non-Hermitian unperturbed Hamiltonian $\hat{H}^{0}$ and some new (also non-Hermitian) perturbation $\hat{V}: \hat{V}$ $=\hat{H}_{\mathrm{BO}}-\hat{H}^{0}$. Using the first-order CHA wave function $\chi$, the generalized Hylleraas functional $J_{2}$ can easily be calculated:

$$
\begin{align*}
& J_{2}=\frac{1}{\left\langle\Psi_{0} \mid \Psi_{0}\right\rangle}\left[2 \operatorname { R e } \left(\langle\hat{Q} \chi| \hat{V}\left|\Psi_{0}\right\rangle\right.\right. \\
&\left.+\operatorname{Re}\left(\langle\chi| \hat{H}^{0}-E_{0}|\chi\rangle\right)\right] \tag{8}
\end{align*}
$$

and the second-order energy will be given by

$$
\begin{equation*}
E^{(2)}=\frac{\left\langle\Psi_{0}\right| \hat{H}_{\mathrm{BO}}\left|\Psi_{0}\right\rangle}{\left\langle\Psi_{0} \mid \Psi_{0}\right\rangle}+J_{2} \tag{9}
\end{equation*}
$$

Here $\Psi_{0}$ is the unperturbed wave function, $E_{0}$ is the zero-order energy ( $\hat{H}^{0} \Psi_{0}=E_{0} \Psi_{0}$ ), and $\hat{Q}$ is the projection operator an to the orthogonal complement to $\Psi_{0}$. These equations define our working formula at the second order perturbation level. This formalism is called "CHA/MP2" theory [42].

## 3. Results and Discussion

The calculations were carried out partly in Heidelberg on a Hewlett-Packard cluster and partly in Debrecen on a Pentium 200 PC and Compaq Alpha running under Linux. The standard HF, MP2 and the CP-corrected HF, MP2 calculations were performed with the Gaussian 98 software [50]. The CHA/CE- and CHA/MP2-type calculations were done by generating the input data (integrals and RHF orbitals) with a slightly modified version of HONDO-8 [51].

In these calculations the CHA/SCF code [30] and the CHA/MP2 program of Mayer and Valiron [42, 44] were used. For the frequency calculations based on Wilson's G-F method, the program written by Beu [52] was applied. The $\mathrm{NH}_{3}-\mathrm{NH}_{3}$ dimer geometries was optimized using conventional Hartree-

Fock and second-order Møller-Plesset perturbation theories for each basis set. We considered different standard Pople basis sets as 6-31G, 6-311G, 6-31++G, $6-311++G, 6-31 G(d, p), 6-311 G(d, p), 6-311++G(d, p)$ $6-311++G(d, p)$, and $6-311++G(2 d, 2 p)$.

The conventional supermolecule geometries were optimized both at HF and MP2 levels applying the analytical gradient method included in Gaussian 98, while the CHA and CP-corrected geometries were calculated by using a numerical gradient method (inverse parabolic interpolation [53]) in internal coordinates. To test the applicability of our numerical gradient method, we performed several sample calculations using both this latter method and the analytical gradient built into Gaussian 98, respectively. As a consequence, there is practically no difference between them for conventional uncorrected cases; we have also performed similar calculations to check the values of the force constans and harmonic vibrational frequencies. The uncorrected HF and MP2 results for the force constants (in internal coordinates) and for the harmonic vibrational frequencies were obtained by using the standard routines of Gaussian 98. As for the CHA and CP-corrected calculations, the numerical second derivatives of the energies were first calculated to obtain the CHA and CP force constants, and then the NOMAD program [52] was applied to obtain the appropriate CHA and CP harmonic vibrational frequencies. As we were interested in the BSSE content in the interaction energies, only those components of the force constant matrix were recalculated which correspond to intermolecular interactions.

The results calculated are summarized in Tables I-III. Table I shows the results obtained for the geometry of the dimer for the conventional, CHA, and Boys-Bernardi schemes both at the HartreeFock and second-order Møller-Plesset perturbation levels of theory. Table II contains the results obtained for the diagonal force constants of the dimer for the uncorrected, CHA, and CP-corrected cases both at the Hartree-Fock and second-order MøllerPlesset perturbation levels of theory. In Table III, we present the conventional, CHA, and CP-corrected results both at the HF and second-order Møller-Plesset perturbation levels of theory for the intermolecular harmonic vibrational frequencies ( $\omega_{2}-\omega_{6}$ ) of the ammonia-ammonia dimer.

A full BSSE-free geometry optimization has been reported by Muguet et al. [2,3] using an a priori BSSE exclusion technique (BSSE-MCSCF) based on the localized molecular orbital method. Their result

TABLE I
Intermolecular coordinates for $\mathrm{NH}_{3} \mathbf{N H}_{3}$ dimer computed at the Hartree-Fock and second-order MHer-Plesset perturbation theory (uncorr., CHA, CP) level, using 6-31G, 6-311G, 6-31 ++G, 6-311++G, $6-31 \mathrm{G}(\mathrm{d}, \mathrm{p}), 6-311 \mathrm{G}(\mathrm{d}, \mathrm{p}), 6-31++\mathrm{G}(\mathrm{d}, \mathrm{p}), 6-311++\mathrm{G}(\mathrm{d}, \mathrm{p})$, and $6-311++\mathrm{G}(2 \mathrm{~d}, 2 \mathrm{p})$ basis sets.

| Basis set | Method | $r_{\text {NN }}(\hat{\text { A }}$ ) |  | $\alpha_{\text {HNN }}$ (deg) |  | $\alpha_{\text {NNH }}$ (deg) |  | Config. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | SCF | MP2 | SCF | MP2 | SCF | MP2 | SCF | MP2 |
| $\begin{array}{r} 6-31 G \\ (30) \end{array}$ | Uncorr. | 3.27044 | 3.15915 | 39.020 | 38.348 | 39.019 | 38.348 | Cyclic | Cyclic |
|  | CHA | 3.32887 | 3.27304 | 85.836 | 87.619 | 5.736 | 5.785 | Asymm. | Asymm. |
|  | CP | 3.35513 | 3.32433 | 83.722 | 84.652 | 6.768 | 7.106 | Asymm. | Asymm. |
| $\begin{gathered} \text { 6-311G } \\ (44) \end{gathered}$ | Uncorr. | 3.25798 | 3.14432 | 39.998 | 39.524 | 39.998 | 39.524 | Cyclic | Cyclic |
|  | CHA | 3.37535 | 3.31263 | 87.197 | 88.504 | 6.154 | 6.403 | Asymm. | Asymm. |
|  | CP | 3.39196 | 3.37575 | 85.832 | 86.249 | 6.694 | 7.547 | Asymm. | Asymm. |
| $6-31++G$ <br> (44) | Uncorr. | 3.31842 | 3.21519 | 88.573 | 78.528 | 6.567 | 12.592 | Asymm. | Asymm. |
|  | CHA | 3.39594 | 3.32434 | 76.032 | 64.922 | 12.843 | 21.186 | Asymm. | Asymm. |
|  | CP | 3.40294 | 3.34718 | 76.800 | 71.385 | 12.452 | 16.822 | Asymm. | Asymm. |
| $\begin{aligned} & 6-311++G \\ & (58) \end{aligned}$ | Uncorr. | 3.32551 | 3.21757 | 92.624 | 81.988 | 5.054 | 10.759 | Asymm. | Asymm. |
|  | CHA | 3.38087 | 3.31480 | 77.584 | 76.027 | 12.457 | 14.218 | Asymm. | Asymm. |
|  | CP | 3.38039 | 3.33264 | 77.633 | 74.330 | 12.649 | 15.612 | Asymm. | Asymm. |
| $\begin{gathered} 6-31 \mathrm{G}(\mathrm{~d}, \mathrm{p}) \\ (60) \end{gathered}$ | Uncorr. | 3.27596 | 3.13437 | 41.234 | 40.647 | 41.234 | 40.647 | Cyclic | Cyclic |
|  | CHA | 3.39126 | 3.30106 | 92.585 | 92.609 | 5.540 | 6.481 | Asymm. | Asymm. |
|  | CP | 3.41875 | 3.33417 | 90.358 | 89.929 | 6.537 | 7.660 | Asymm. | Asymm. |
| $\begin{aligned} & \text { 6-311G(d,p) } \\ & (74) \end{aligned}$ | Uncorr. | 3.28708 | 3.11678 | 41.784 | 41.244 | 41.783 | 41.244 | Cyclic | Cyclic |
|  | CHA | 3.45301 | 3.32905 | 92.333 | 92.104 | 6.568 | 7.890 | Asymm. | Asymm. |
|  | CP | 3.48886 | 3.38795 | 91.292 | 90.577 | 6.867 | 8.309 | Asymm. | Asymm. |
| $\begin{aligned} & 6-31++G(d, p) \\ & (74) \end{aligned}$ | Uncorr. | 3.40270 | 3.23422 | 87.783 | 85.780 | 10.063 | 12.466 | Asymm. | Asymm. |
|  | CHA | 3.44118 | 3.31066 | 77.128 | 73.363 | 15.170 | 19.114 | Asymm. | Asymm. |
|  | CP | 3.44586 | 3.31185 | 77.180 | 69.866 | 14.914 | 20.916 | Asymm. | Asymm. |
| $\begin{aligned} & 6-311++G(d, p) \\ & (88) \end{aligned}$ | Uncorr. | 3.44761 | 3.25961 | 90.992 | 91.413 | 8.629 | 10.082 | Asymm. | Asymm. |
|  | CHA | 3.47140 | 3.31352 | 80.070 | 76.171 | 13.703 | 17.136 | Asymm. | Asymm. |
|  | CP | 3.46760 | 3.31682 | 80.130 | 73.615 | 13.838 | 18.857 | Asymm. | Asymm. |
| $\begin{aligned} & 6-311++G(2 d, 2 p) \\ & (118) \end{aligned}$ | Uncorr. | 3.49518 | 3.25790 | 83.116 | 78.799 | 12.686 | 15.908 | Asymm. | Asymm. |
|  | CHA | 3.50573 | 3.28425 | 81.003 | 75.933 | 13.594 | 17.412 | Asymm. | Asymm. |
|  | CP | 3.50137 | 3.27440 | 78.695 | 68.033 | 14.954 | 22.099 | Asymm. | Asymm. |

also shows an intermediate geometry configuration, but the $\alpha_{\mathrm{HNN}}=53.2^{\circ}$ and $\alpha_{\mathrm{NNH}}=39.7^{\circ}$ (Fig. 1a) are much closer to the cyclic structure than the linear hydrogen-bonded one, while our values are closer to the linear configuration ( $\alpha_{\mathrm{HNN}}=75.9^{\circ}$ and $\alpha_{\mathrm{NNH}}=17.4^{\circ}$ in CHA using $6-311 \mathrm{G}++(2 \mathrm{~d}, 2 \mathrm{p})$ at the MP2 level at theory).

The $r_{\mathrm{NN}}$ intermolecular distance also shows an important BSSE dependence, but this effect became smaller and smaller in case of using large and wellbalanced basis sets and came near the experimental value ( $r_{\mathrm{NN}}=3.337 \AA$ ) [11]. Moreover, it is very important to note that the existence of cyclic configurations (Fig. 1b) as the global minimum symmetry is definitely a BSSE effect. When a BSSE-free optimization technique is used, this configuration becomes only a transition-state structure.

Another significant remark is that when density functional theory methods are used, the intermediate configuration is very difficult to obtain; in almost all cases, the linear-bonded hydrogen structure were preferred $[5,6]$.

Considering the results, the following conclusions can be drawn:

1. As can be expected, the BSSE-free CP and CHA interaction energies usually show less deep minima than those obtained from the uncorrected methods both at the HF and at the second-order Møller-Plesset perturbation level of theory. From Table II it can be concluded that apart from a few cases the values of the intermolecular diagonal force constans are significantly larger in the uncorrected

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TABLE II
Intermolecular force constants for the $\mathrm{NH}_{3}-\mathrm{NH}_{3}$ dimer computed at the Hartree-Fock and second-order Møller-Plesset perturbation theory (Uncorr., CHA, CP) level, using 6-31G, 6-311G, 6-31++G, 6-311++G, $6-31 \mathrm{G}(\mathrm{d}, \mathrm{p}), 6-311 \mathrm{G}(\mathrm{d}, \mathrm{p}), 6-31++\mathrm{G}(\mathrm{d}, \mathrm{p}), 6-311++\mathrm{G}(\mathrm{d}, \mathrm{p})$, and $6-311++\mathrm{G}(2 \mathrm{~d}, 2 \mathrm{p})$ basis sets.

| Basis set | Method | $f_{r r}$ (a.u./A ${ }^{2}$ ) |  | $f_{\alpha_{1} \alpha_{1}}\left(\right.$ a.u. $\left./ \operatorname{Rad}^{2}\right)$ |  | $f_{\alpha_{2} \alpha_{2}}\left(\right.$ a.u. $\left./ \operatorname{Rad}^{2}\right)$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | SCF | MP2 | SCF | MP2 | SCF | MP2 |
| $\begin{array}{r} 6-31 G \\ (30) \end{array}$ | Uncorr. | . 020959 | . 031705 | . 029226 | . 039164 | . 029116 | . 039164 |
|  | CHA | . 026128 | . 026053 | . 013131 | . 014801 | . 037030 | . 043124 |
|  | CP | . 017096 | . 020452 | . 012212 | . 014838 | . 035060 | . 044515 |
| $6-311 G$ <br> (44) | Uncorr. | . 019896 | . 028001 | . 028340 | . 037001 | . 028339 | . 037001 |
|  | CHA | . 020664 | . 023314 | . 011556 | . 013189 | . 033747 | . 040037 |
|  | CP | . 016672 | . 019060 | . 013131 | . 013000 | . 033616 | . 036505 |
| $6-31++G$ <br> (44) | Uncorr. | . 019300 | . 028067 | . 014563 | . 015793 | . 041412 | . 046379 |
|  | CHA | . 014080 | . 018001 | . 012765 | . 017692 | . 032732 | . 035477 |
|  | CP | . 014424 | . 017531 | . 012433 | . 015035 | . 032529 | . 036372 |
| $\begin{aligned} & 6-311++G \\ & (58) \end{aligned}$ | Uncorr. | . 019290 | . 027378 | . 015322 | . 013708 | . 042041 | . 043462 |
|  | CHA | . 015558 | . 018595 | . 013025 | . 015293 | . 032383 | . 037885 |
|  | CP | . 015132 | . 018056 | . 012890 | . 014686 | . 032720 | . 037056 |
| $\begin{gathered} 6-31 \mathrm{G}(\mathrm{~d}, \mathrm{p}) \\ (60) \end{gathered}$ | Uncorr. | . 019350 | . 028546 | . 022292 | . 028567 | . 022293 | . 028567 |
|  | CHA | . 019060 | . 023498 | . 008929 | . 009895 | . 026525 | . 030508 |
|  | CP | . 015600 | . 019712 | . 008010 | . 010374 | . 026525 | . 033485 |
| $\begin{aligned} & \text { 6-311G(d,p) } \\ & (74) \end{aligned}$ | Uncorr. | . 017829 | . 027752 | . 020948 | . 027653 | . 020949 | . 027654 |
|  | CHA | . 021340 | . 021716 | . 007616 | . 008699 | . 022717 | . 027574 |
|  | CP | . 013440 | . 017416 | . 006434 | . 008535 | . 021141 | . 026525 |
| $6-31++G(d, p)$ <br> (74) | Uncorr. | . 015886 | . 025999 | . 009571 | . 011179 | . 027586 | . 036429 |
|  | CHA | . 012666 | . 017393 | . 010111 | . 011271 | . 023768 | . 028468 |
|  | CP | . 012956 | . 017512 | . 009323 | . 010899 | . 023374 | . 027050 |
| $\begin{aligned} & 6-311++G(d, p) \\ & (88) \end{aligned}$ | Uncorr. | . 013463 | . 022475 | . 008407 | . 009974 | . 024836 | . 034293 |
|  | CHA | . 012048 | . 016426 | . 008010 | . 009962 | . 021667 | . 027150 |
|  | CP | . 012140 | . 016868 | . 008010 | . 010374 | . 021273 | . 026262 |
| $\begin{aligned} & 6-311++G(2 d, 2 p) \\ & (118) \end{aligned}$ | Uncorr. | . 010893 | . 019707 | . 006704 | . 008705 | . 020386 | . 029553 |
|  | CHA | . 010229 | . 017751 | . 006855 | . 009093 | . 019781 | . 027635 |
|  | CP | . 010242 | . 017790 | . 007059 | . 010601 | . 019592 | . 026188 |

case. In spite of this tendency, sometimes the opposite effect also occurs, especially when the basis sets used are not large enough. We must emphasize that the results are very sensitive to the applied basis sets and some of them, such as $6-31 G, 6-31 G(d, p)$, etc., are not really appropriate to describe the structure and the molecular properties. But when diffuse or diffuse and polarization functions are used in the applied basis sets, in practically all cases the counterpoise-corrected results are fairly close to those given by the CHA-based methods for all studied quantities. Concerning the calculation of the harmonic vibrational frequencies, there is no unambiguous tendency between the corrected and uncorrected results because the frequency values can
strongly depend upon the modified dimer geometries.
2. We also note that agreement between the CP and CHA-corrected results both at the HF and at correlated levels is very good. This observation is consistent with our previous studies in the field of intermolecular interactions. Similarly to our earlier results, the difference between the uncorrected and corrected values becomes smaller for large enough basis sets as the values of the intermolecular interactions converge.
3. It is also interesting to note, however, that the values of the diagonal force constants and harmonic vibrational frequencies of ammo-nia-ammonia dimer calculated at the correlated level are larger than those obtained from

TABLE III
Intermolecular frequencies for the $\mathrm{NH}_{3}-\mathrm{NH}_{3}$ dimer computed at the Hartree-Fock and second-order MøllerPlesset perturbation theory (Uncorr., CHA, CP) level, using 6-31G, 6-311G, 6-31++G, 6-311++G, 6-31G(d,p), $6-311 G(d, p), 6-31++G(d, p), 6-311++G(d, p)$, and $6-311++G(2 d, 2 p)$ basis sets.

| Basis set | Method | $\omega_{2}\left(\mathrm{~cm}^{-1}\right)$ |  | $\omega_{3}\left(\mathrm{~cm}^{-1}\right)$ |  | $\omega_{4}\left(\mathrm{~cm}^{-1}\right)$ |  | $\omega_{5}\left(\mathrm{~cm}^{-1}\right)$ |  | $\omega_{6}\left(\mathrm{~cm}^{-1}\right)$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | SCF | MP2 | SCF | MP2 | SCF | MP2 | SCF | MP2 | SCF | MP2 |
| $\begin{array}{r} \text { 6-31G } \\ (30) \end{array}$ | Uncorr. | 104.8 | 126.5 | 131.9 | 161.4 | 145.7 | 182.6 | 247.7 | 279.1 | 470.8 | 526.7 |
|  | CHA | 126.3 | 132.7 | 150.6 | 155.0 | 209.9 | 234.7 | 355.7 | 374.5 | 515.0 | 539.4 |
|  | CP | 107.6 | 127.5 | 127.4 | 163.1 | 218.1 | 249.4 | 428.1 | 465.1 | 614.2 | 663.0 |
| 6-311G <br> (44) | Uncorr. | 98.9 | 117.1 | 128.9 | 151.2 | 131.5 | 158.0 | 245.2 | 270.4 | 482.5 | 527.4 |
|  | CHA | 118.1 | 125.3 | 142.1 | 155.0 | 206.9 | 227.3 | 365.7 | 381.3 | 496.8 | 523.2 |
|  | CP | 115.7 | 116.9 | 150.6 | 145.9 | 215.4 | 239.4 | 428.0 | 439.8 | 583.2 | 601.7 |
| $6-31++G$ <br> (44) | Uncorr. | 125.9 | 119.8 | 135.0 | 141.0 | 138.6 | 155.6 | 292.7 | 296.9 | 404.7 | 449.5 |
|  | CHA | 80.5 | 61.6 | 87.5 | 103.5 | 113.1 | 124.7 | 224.9 | 230.3 | 395.3 | 430.0 |
|  | CP | 81.9 | 76.6 | 89.7 | 118.4 | 114.7 | 126.6 | 225.8 | 244.2 | 393.9 | 427.0 |
| $6-311++G$ <br> (58) | Uncorr. | 125.9 | 114.9 | 144.6 | 149.4 | 149.5 | 156.7 | 313.9 | 306.4 | 421.6 | 436.0 |
|  | CHA | 75.0 | 92.5 | 93.1 | 123.1 | 117.5 | 129.9 | 237.3 | 253.7 | 404.8 | 436.9 |
|  | CP | 74.0 | 88.3 | 93.0 | 118.1 | 118.6 | 127.5 | 237.1 | 247.8 | 404.7 | 430.0 |
| $\begin{gathered} 6-31 \mathrm{G}(\mathrm{~d}, \mathrm{p}) \\ (60) \end{gathered}$ | Uncorr. | 89.8 | 107.1 | 118.6 | 140.0 | 127.0 | 151.6 | 231.9 | 254.5 | 437.6 | 473.9 |
|  | CHA | 106.4 | 111.1 | 134.9 | 149.3 | 189.7 | 203.6 | 374.4 | 389.1 | 550.3 | 547.5 |
|  | CP | 93.6 | 120.5 | 120.7 | 148.3 | 193.0 | 208.1 | 376.3 | 405.0 | 623.0 | 605.2 |
| $\begin{aligned} & \text { 6-311G(d,p) } \\ & (74) \end{aligned}$ | Uncorr. | 88.2 | 120.6 | 116.4 | 135.9 | 122.4 | 151.1 | 222.1 | 246.1 | 423.8 | 463.0 |
|  | CHA | 100.3 | 97.9 | 140.2 | 146.1 | 185.0 | 197.5 | 347.7 | 370.1 | 516.3 | 510.9 |
|  | CP | 77.8 | 100.9 | 112.2 | 134.4 | 189.8 | 202.8 | 339.4 | 367.0 | 589.1 | 555.5 |
| $\begin{aligned} & 6-31++G(d, p) \\ & (74) \end{aligned}$ | Uncorr. | 95.6 | 105.9 | 114.6 | 127.4 | 123.6 | 155.2 | 251.8 | 286.8 | 383.5 | 424.1 |
|  | CHA | 78.3 | 49.4 | 89.0 | 99.2 | 117.6 | 131.5 | 202.9 | 226.0 | 377.1 | 404.3 |
|  | CP | 71.1 | 37.6 | 90.0 | 93.3 | 118.3 | 130.7 | 210.2 | 226.5 | 364.1 | 394.1 |
| $\begin{aligned} & 6-311++G(d, p) \\ & (88) \end{aligned}$ | Uncorr. | 90.5 | 102.3 | 114.7 | 131.7 | 116.0 | 146.8 | 248.3 | 290.3 | 363.3 | 407.2 |
|  | CHA | 65.3 | 59.3 | 85.3 | 95.0 | 109.3 | 125.1 | 197.2 | 219.8 | 355.6 | 388.7 |
|  | CP | 59.2 | 62.3 | 84.6 | 88.5 | 110.7 | 131.2 | 202.7 | 221.5 | 347.6 | 380.3 |
| $\begin{aligned} & 6-311++G(2 d, 2 p) \\ & (118) \end{aligned}$ | Uncorr. | 65.2 | 65.3 | 100.2 | 110.1 | 104.7 | 137.6 | 218.1 | 248.1 | 335.3 | 390.7 |
|  | CHA | 63.0 | 57.4 | 96.0 | 104.9 | 101.5 | 129.2 | 205.4 | 229.0 | 339.0 | 392.5 |
|  | CP | 60.9 | 52.7 | 91.3 | 93.4 | 102.2 | 129.9 | 195.7 | 202.0 | 339.4 | 393.8 |

the Hartree-Fock calculation. This behavior is a direct consequence of the fact that, at the correlated level, the interactions between the molecules are much stronger.
4. In the BSSE-corrected calculations, both the HF and MP2 levels of the cyclic state of the ammonia-ammonia dimer disappeared and instead, a new, so-called intermediate asymmetric configuration is preferred. On the other hand, by using diffuse functions in the basis set, the quasilinear geometry of the dimer is distorted, and an intermediate configuration is favored.
5. Focusing to the correlated level, the amount of BSSE in the intermolecular interaction energies is much larger than that at the HF level, and this effect is also conserved in the values
of the force constants and harmonic vibrational frequencies. All these results clearly indicate the importance of the proper BSSE-free correlation treatment with the well-defined basis functions.

In this paper we performed calculations for the geometries, force constants, and the intermolecular harmonic vibrational frequencies of the ammonia dimers. The calculations have been taken at both Hartree-Fock and correlated (second-order MøllerPlesset perturbation theory) levels of theory in several different basis sets. Comparisons have been made between the a posteriori Boys-Bernardi "counterpoise" correction scheme and the a priori "chemical Hamiltonian approach." It can be concluded from the results that there is practically no


FIGURE 1. (a) Asymmetric structure of the ammoniaammonia dimer. (b) Cyclic structure of the ammoniaammonia dimer.
difference between these two methods, so the a priori CHA scheme can be considered as an ultimate solution of the BSSE problem. We also found that the basis set superposition error influence is fairly significant in the studied quantities, so removing this effect is very important.

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